

# 七年级下学期第一次月考考试数学试题

(120分钟, 满分150)

## 一、选择题 (12×4=48分)

|    |   |   |   |   |   |   |   |   |   |    |    |    |
|----|---|---|---|---|---|---|---|---|---|----|----|----|
| 题号 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 答案 | B | B | B | B | D | B | B | C | B | B  | A  | C  |

## 二、填空题 (6×4=24分)

13. 2, 4      14. (0, 15)      15. 60

16. 如果两个角是同一角的补角, 那么这两个角相等      18.  $\frac{1}{3}$

## 三、解答题 (共78分)

19. (本题10分) 计算:

|  |   |
|--|---|
| <p>(1) <math> \sqrt{2} - \sqrt{3}  + \sqrt[3]{8} + 2(\sqrt{3} - 1)</math></p> <p>解: 原式 = <math>-\sqrt{2} + \sqrt{3} + 2 + 2\sqrt{3} - 2</math></p> <p style="text-align: center;"><math>= -\sqrt{2} + 3\sqrt{3}</math></p> | <p>(2) <math>(\sqrt{6})^2 + \sqrt{9} - \sqrt[3]{-8}</math></p> <p>原式 = <math>6 + 3 - (-2)</math></p> <p style="text-align: center;"><math>= 9 + 2</math></p> <p style="text-align: center;"><math>= 11</math></p> |
|--|---|

20. (本题10分) 求下列x的值:

|   |  |
|---|--|
| <p>解: (1) <math>4(3x+1)^2 - 1 = 0;</math></p> <p style="text-align: center;"><math>(3x+1)^2 = \frac{1}{4}</math></p> <p style="text-align: center;"><math>3x+1 = \pm \frac{1}{2}</math></p> <p style="text-align: center;"><math>3x+1 = \frac{1}{2} \text{ 或 } 3x+1 = -\frac{1}{2}</math></p> <p style="text-align: center;"><math>\therefore x = -\frac{1}{6} \text{ 或 } x = -\frac{1}{2}</math></p> | <p>(2) <math>\frac{1}{2}(x+3)^3 = 4</math></p> <p style="text-align: center;"><math>(x+3)^3 = 8</math></p> <p style="text-align: center;"><math>x+3 = \sqrt[3]{8}</math></p> <p style="text-align: center;"><math>x+3 = 2</math></p> <p style="text-align: center;"><math>\therefore x = -1</math></p> |
|---|--|



21. (本题 10 分)

解: 设不同意小明的说法.

设长方形纸片的长为  $3x$  cm, 宽为  $2x$  cm. ( $x > 0$ )

由题意得  $3x \cdot 2x = 300$

$$6x^2 = 300$$

$$x^2 = 50$$

$$x = \pm\sqrt{50}$$

$$\because x > 0$$

$$\therefore x = \sqrt{50}$$

$$\therefore 3x = 3\sqrt{50}$$

$$\therefore \sqrt{50} > 7$$

$$\therefore 3\sqrt{50} > 21$$

即长方形的长大于 21 cm

$$\because \sqrt{400} = 20$$

$\therefore$  正方形的边长为 20 cm

$$\therefore 3\sqrt{50} > 20$$

$\therefore$  长方形纸片的长大于正方形的边长

$\therefore$  不能裁出.

22. (本题 12 分)

(1)

解: 由题意得

$$2a - 1 = 9, 3a + b - 9 = 8, 0 = 4.$$

解得  $a = 5, b = -2, c = 4$

$$\therefore a + 2b + c = 5 + 2 \times (-2) + 4 = 5$$

(2) 已知点  $P(2m+4, m-1)$ , 请分别根据下列条件, 求出点  $P$  的坐标.

① 解: 由题意得

$$2m + 4 - 6 = m - 1$$

$$\therefore m = 1$$

$$\therefore 2m + 4 = 2 \times 1 + 4 = 6, m - 1 = 1 - 1 = 0$$

$$\therefore P(6, 0)$$

② 由题意得

$$2m + 4 = 2$$

$$\therefore m = -1$$

$$\therefore m - 1 = -1 - 1 = -2 \therefore P(2, -2)$$

③ 由题意得

$$|2m + 4| = |m - 1|$$

$$\therefore 2m + 4 = m - 1 \text{ 或 } 2m + 4 = -(m - 1)$$

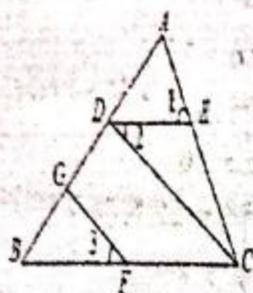
$$\therefore m = -5 \text{ 或 } m = -1$$

$$\text{当 } m = -5 \text{ 时 } 2m + 4 = 2 \times (-5) + 4 = -6 \therefore P(-6, -6)$$

$$\text{当 } m = -1 \text{ 时 } 2m + 4 = 2 \times (-1) + 4 = 2 \therefore P(2, -2)$$

综上所述得  $P(-6, -6)$  或  $(2, -2)$

23、(本题 10 分)



证明:  $\because \angle 1 = \angle ACB$

$\therefore DE \parallel BC$

$\therefore \angle 2 = \angle DCB$

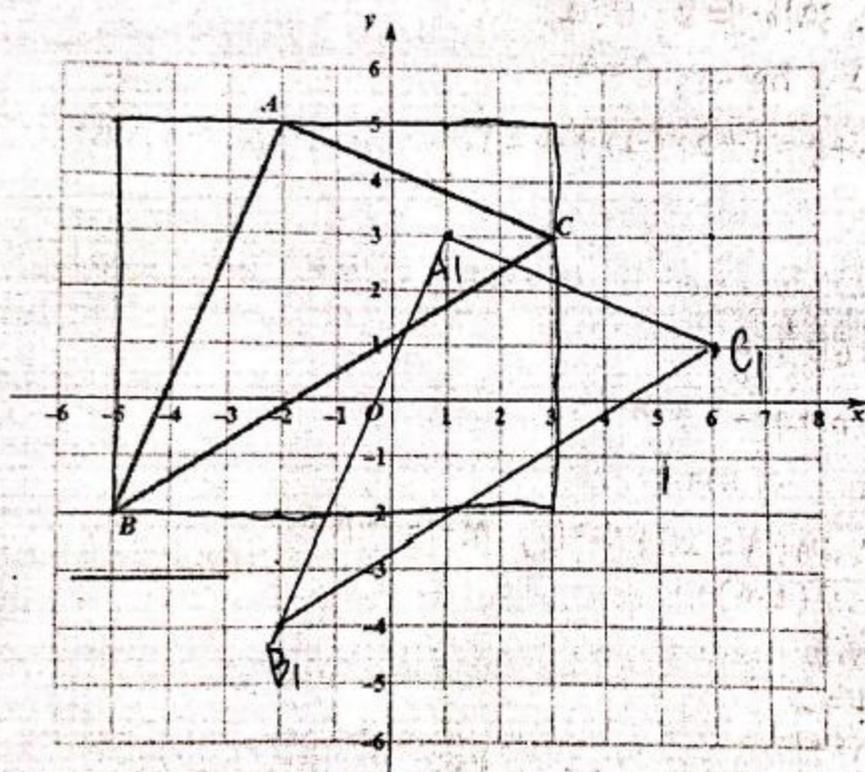
又  $\because \angle 2 = \angle 3$

$\therefore \angle DCB = \angle 3$

$\therefore DC \parallel GF$

$\therefore \angle BDC + \angle DGF = 180^\circ$

24、(本题 12 分)

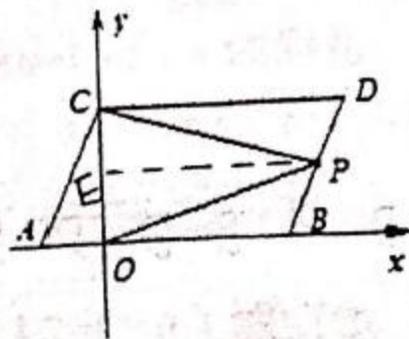
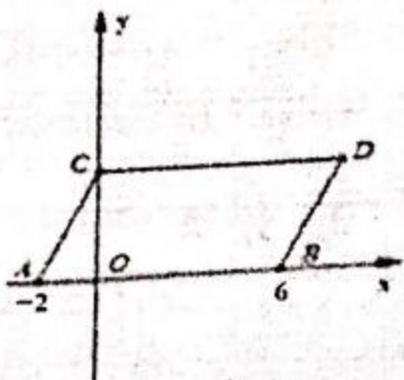


解: (1)  $A(-2, 5)$   $B(-5, -2)$   $C(3, 3)$  ----- 3'

(2)  $S_{\triangle ABC} = 8 \times 7 - \frac{1}{2} \times 3 \times 7 - \frac{1}{2} \times 2 \times 5 - \frac{1}{2} \times 5 \times 8$  ----- 3'  
 $= 56 - 10.5 - 5 - 20$   
 $= 20.5$

(3) 如图所示  $\triangle A_1B_1C_1$  即为所求 ----- 3'

$A_1(1, 3)$ ,  $B_1(-2, -4)$ ,  $C_1(6, 1)$  ----- 3'



4' 解: (1) 由题意可得  $C(-2+2, 0+4)$   $D(6+2, 0+4)$   
即  $C(0, 4)$   $D(8, 4)$

(2) 由题意可知四边形 ABCD 为平行四边形.

$$\therefore S_{\text{四边形}ABDC} = AB \cdot OC = 8 \times 4 = 32$$

5' ① - (2) 拓展.

设  $P(0, y)$

$$\therefore S_{\triangle PAB} = S_{\text{四边形}ABDC} = 32$$

$$\textcircled{4}' \quad \therefore \frac{1}{2} AB \cdot |y| = 32$$

$$\therefore \frac{1}{2} \times 8 \times |y| = 32$$

$$\therefore |y| = 8$$

$$\therefore y = \pm 8$$

$$\therefore P(0, 8) \text{ 或 } P(0, -8)$$

⑤ (3) 结论①正确.

过点 P 作  $PE \parallel AB$  交 y 轴于 E  
由平移性质所得  $AB \parallel CD$

$$\therefore PE \parallel AB \parallel CD$$

$$\therefore \angle DCP = \angle CPE, \angle POB = \angle EPO$$

$$\text{又} \because \angle CPO = \angle CPE + \angle EPO$$

$$\therefore \angle CPO = \angle DCP + \angle POB \quad \therefore \frac{\angle DCP + \angle POB}{\angle CPO} = 1$$